

Computer Simulation and Control of a Theoretical Coagulation pH System in Water Treatment

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Abstract. Coagulation is an important process in water treatment operations. Inorganic coagulants such as aluminium salts consume alkalinity and may necessitate the addition of alkaline agent such as lime during coagulation. The pH required for coagulation is very critical. Particularly, aluminium salts serving as a basis for this work are most effective around a pH range of 5.5-6.5. It is therefore vital to attain this pH after the coagulant has been added. In this study, a typical coagulation pH control application called CoagiT has been developed. CoagiT seeks to maintain the optimum pH necessary for effective coagulation in water treatment. The application was developed particularly for application in Ghana using instrumentation and control principles and Visual Basic (VB) programming algorithms. This application can enhance learning by integrating the theoretical cogitation of control process with tactile nature of the plant. The application can operate in both closed-loop manual and automatic control modes. In the manual mode, when the measured pH value of the coagulation water is not equal to the set point pH, the application alerts an operator (by sounding an alarm) and suggests the percentage by which the lime supply rate should be adjusted to achieve the set point. In the automatic mode, the application automatically adjusts the lime supply rate to achieve the set point pH with the help of a pH transmitter and a pH indicating controller. CoagiT may be a useful simulation tool to provide user graphical windows environment in reducing the problems associated with ineffective coagulation due to improper pH control during water treatment.

Keywords: coagulation, pH, computer simulation, visual basic programming, process control, water treatment

1 Introduction

Coagulation is an important process in water treatment operations. It forms the basis of the entire water treatment process and as such, it can have a significant impact (positive or negative) on the performance of downstream process units [1]. Coagulation involves the destabilisation and subsequent aggregation of suspended and colloidal particles from raw water owing to the addition of chemical coagulants [2]. Effective coagulation is vital to achieve operational efficiency of water treatment plants, compliance with standards set by regulatory agencies and provision of consistent potable water for consumption. Otherwise, the water treatment process will result in wastage of expensive chemicals, poor floc formation, less efficient filtration and health hazards to final consumers [3]. The key issue about the process is that, coagulants functions effectively only within a specified pH range hence, the efficacy of the coagulation process depends on proper control of raw water pH [4].

Coagulation is effective within a feed water pH of 5.5-6.5 for alum salts and pH of 4.5-5.5 for ferric chloride salts [5]. Addition of inorganic coagulants to feed water mostly consume the alkalinity of the feed water and hence decreases the pH of the feed water [6]. In order to counter-act the effect of coagulants on pH and ensure effective coagulation, most water treatment facilities use pH control methods such as the addition of lime to adjust and maintain the pH to the optimal range [6].

Adjusting the lime feed rate to achieve the optimal pH range or set point for effective coagulation is difficult and exhausting and often involves the use of the trial and error approach, which is particularly the case in some water treatment facilities in Ghana. As a result, a more reliable, accurate and efficient control system based on a computer programming software is needed. This software together with analytical sensors should be able to automatically adjust the pH of the feed water to its set point by

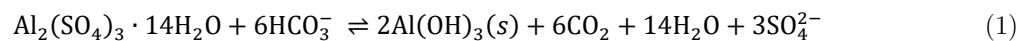
adjusting and controlling the lime dose rate. Also, it should be able to alert operators to dose in the correct amount of lime that would adjust the pH to the set point when operating in the manual mode. Most water treatment facilities in Ghana, however, do not have any control system for pH control during coagulation [7].

This study therefore, seeks to enhance process control education with simulation of a coagulation pH control system, to control the pH of the feed water during coagulation in water treatment systems, by adopting and modifying the Process Flow Diagram (PFD) shown in Figure 1 using Visual Basic programming language.

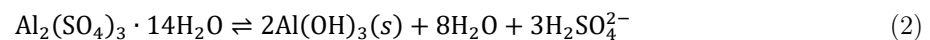
2 Background

2.1 Chemical Coagulation and pH Control

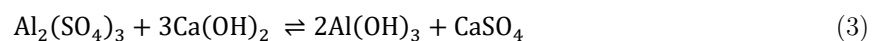
Most metal coagulants generate an acidic environment when introduced in water [8], and therefore their addition consumes alkalinity. For example, when alum is used as a coagulant, it hydrolyses and forms aluminium hydroxide floc by reacting with the natural alkalinity (usually consists of bicarbonate), as expressed by Equation 1, with the insoluble products (precipitates) in italics [9]:



Each mole of hydrated aluminium sulphate added consumes six (6) moles of alkalinity and produces six mole of carbon dioxide. The above reaction shifts the carbonate equilibrium and decreases the pH. Nevertheless, as long as sufficient alkalinity is present and $\text{CO}_2(\text{g})$ is allowed to evolve, the pH is not drastically reduced and is generally not an operational problem. Bourke *et al.* [9] indicated that, a 1 mg/L dose of alum reacts with 0.53 mg/L of alkalinity expressed as CaCO_3 . Therefore, coagulant addition into waters with low alkalinity may produce sulphuric acid (Equation 2) leading to the consumption of all the alkalinity available in the water and reducing the pH to a value too low for effective coagulation [6, 8]:



In such a situation, additional alkali such as hydrated lime $\{\text{Ca}(\text{OH})_2\}$, is added to supply the water with the necessary alkalinity required to produce the aluminium hydroxide floc needed for effective coagulation. This can be expressed by Equation 3.



The metal hydroxide flocs formed with the use of inorganic coagulants (such as alum) are known to be insoluble over relatively narrow bands of pH, which may vary with the source of the raw water [6, 9]. Therefore, the pH at which coagulation occurs is the most important parameter for proper coagulation performance [6, 10]. The latter implies that pH control (In a real plant it is not only the process control, but the parameter of concern in this work) is necessary for effective coagulation. Proper pH control does not only help in efficient removal of turbidity and colour, but also help to maintain satisfactory minimum levels of dissolved residual aluminium in the clarified water [9]. Studies by Hu *et al.* [11] also indicated that proper pH control during coagulation is essential to:

- a) Increase the removal of natural organic matter (NOM) from raw water when using alum;
- b) Improve the coagulation process by regulating metal species distributions;
- c) Significantly improve the coagulation efficiency of AlCl_3 in eutrophic waters;
- d) Reduce wastage of chemicals;
- e) Obtain good floc formation;
- f) Increase efficient filtration; and
- g) Reduce health hazards to final consumers.

2.2 Theory and Principle Behind Coagulation

The software was developed by modifying and simulating the Process Flow Diagram (PFD) of the coagulation pH control system shown in Figure 1. In the PFD shown, raw water (influent) and coagulant flow into a mixing chamber containing a motor-controlled mixing agitator for rapid mixing of solution.

The solution moves into a contact zone with a pH transmitter (AT) to measure the pH of the solution and transmit this measured pH in its equivalent electrical signal (4-20 mA) to a pH indicating controller (AIC). The pH indicating controller compares the signal from the pH transmitter to a set point (SP) within the AIC and sends a control signal based on the difference between the measured signal and the set point (i.e. the error) to a variable speed drive of a conveyor to adjust its speed, this subsequently controls the lime feed rate into the mixing chamber. This simple feedback mechanism is the fundamental framework guiding the operation of the simulation software.

To consider how this feedback control strategy could be implemented, a block diagram (closed loop control) for the coagulation pH control system is shown in Figure 2. For the coagulation pH under feedback control (Figure 1), the pH $y(s)$ is controlled and the lime reagent flow rate r_2 is adjusted using proportional control. The operation of this feedback control system can be summarised as follows:

- I. *Analyser and transmitter:* The mixing tank $pH(y(s))$ is measured by an analyser and then the measurement is converted to a corresponding electrical current signal by a transmitter.
- II. *Feedback control:* The controller performs three distinct calculations. First, it converts the actual pH set point $X_{sp(s)}$ into an equivalent internal signal i_{sp} . Second, it calculates an error signal $e(s)$ by subtracting the measured value $y_m(s)$ from the set point corresponding signal i_{sp} , that is $e(s) = i_{sp} - y_m(s)$. Third, controller output $c(s)$ is calculated from the proportional control law.
- III. *Lime conveyor motor:* The controller output $c(s)$ in this case an electrical current signal is sent to the conveyor motor (lime reagent conveyor motor) to adjust the percentage speed of the conveyor, which affects flow rate $r_2(s)$.

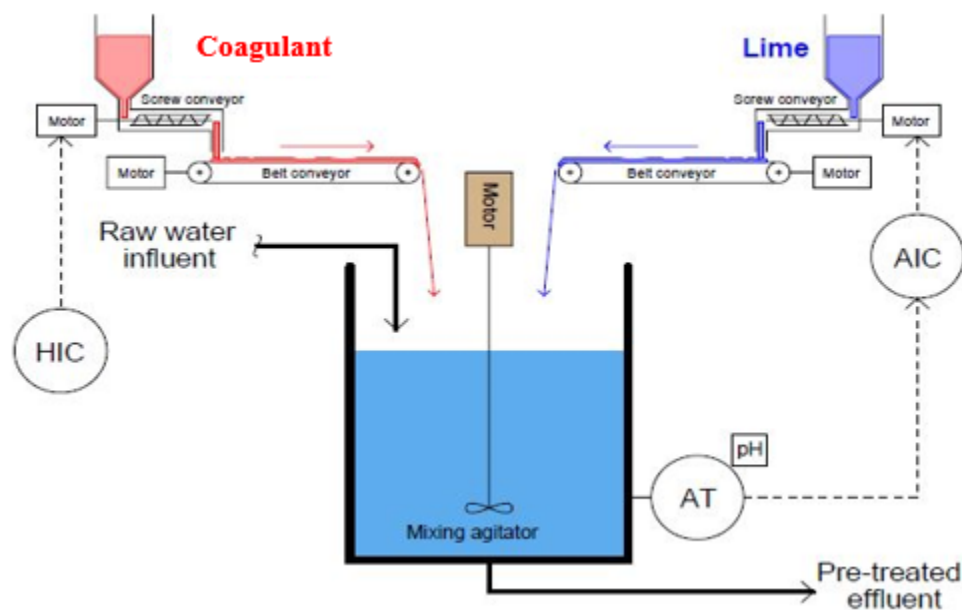


Figure 1. PFD of a coagulation pH control system [12]

The mathematical expression or the transfer function showing the closed loop response (Figure 2) is given by Equation 4:

$$y(s) = \frac{Ga(s)Gc(s)Gp(s)Gv(s)}{1+Gc(s)Gm(s)Gp(s)Gv(s)} \cdot X_{sp}(s) + \frac{r_1(s)Gp(s)}{1+Gc(s)Gm(s)Gp(s)Gv(s)} + \frac{DGg(s)Gp(s)}{1+Gc(s)Gm(s)Gp(s)Gv(s)} \quad (4)$$

where, $Ga(s)$ is the transfer function of analyser calibrator in the controller, $Gc(s)$ is the transfer function of the controller, $Gv(s)$ is the transfer function of the lime conveyor motor, $Gg(s)$ is the transfer function of coagulant reagent conveyor motor, $Gp(s)$ is the transfer function of the process in the mixing tank, $Gm(s)$ is the transfer function of the sensor (feedback) and $f(s)$ is the total flow mixture of raw water and coagulant before addition of lime going into the mixing tank.

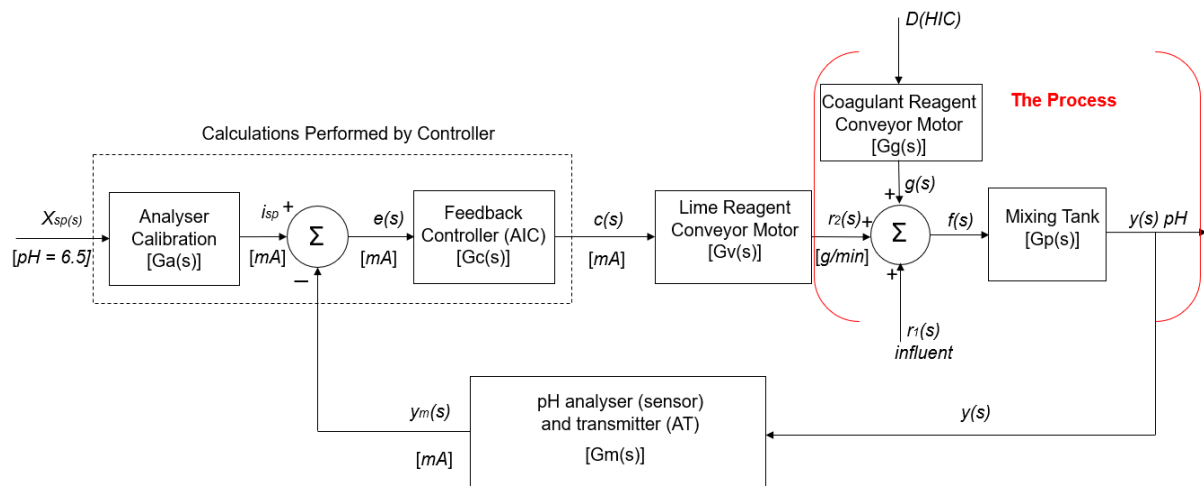


Figure 2. Block diagram for the coagulation feedback control system in Figure 1

3 Resources and Method Used

3.1 Designing and Testing of CoagiT

CoagiT was developed mainly to measure the coagulation pH of water and ensure that the pH is within the set point by adjusting the lime dose rate. This ensures effective coagulation and eliminates the problems (poor floc formation, less efficient filtration, health hazards to final consumers and non-compliance with government agencies) associated with ineffective coagulation. CoagiT operates using the equations and interpolations outlined below.

3.1.1 Measured signal-measured value conversion

Equation 5 was used in the programme to convert the measured signal (in milli-amperes) of the analytical transmitter to a measured pH value [7,12]. This allows for the comparison of the measured value with the set point.

$$MV = \left[\left(\frac{MS - LRV_s}{Span_s} \right) \times (Span_m) \right] + LRV_m \quad (5)$$

where;

- MV = Measured value
- MS = Measured signal
- LRV_s = Lower Range Value of the transmitter signal
- $Span_s$ = Span of transmitter signal
- $Span_m$ = Span of measurement
- LRV_m = Lower Range Value of measurement

3.1.2 Error calculation

CoagiT uses the difference between the measured value and the set point to adjust the lime feed rate. This difference is called the error and Equation 6 shows how it is calculated [7].

$$Error = |SP - MV| \quad (6)$$

where;

- SP = Set point
- MV = Measured value

3.1.3 Motor speed adjustment

The speed of the lime conveyor motor is adjusted using Equation 7.

$$\text{Speed (\%)} = \frac{|\text{SP}-\text{MV}|}{\text{SP}} \times 100 \tag{7}$$

where;

SP = Set point

MV = Measured value

3.1.4 Motor speed-lime flow rate conversion

Each motor speed calculated corresponds to a given flow rate of the lime. Equation 8 was used to convert the motor speed (in percentage) to the corresponding lime feed rate (in grams per minute).

$$\text{LFR} = \left[\left(\frac{\text{Speed}-\text{LRV}_{\text{speed}}}{\text{Span}_{(\text{speed})}} \right) \times (\text{Span}_{\text{LFR}}) \right] + \text{LRV}_{\text{LFR}} \tag{8}$$

where;

LFR = Lime feed rate

LRV_{speed} = Lower Range Value of the motor speed

LRV_{LFR} = Lower Range Value of the lime feed rate

Span_(speed) = Span of the motor speed

Span_(LFR) = Span of lime feed rate

3.2 Designing of CoagiT

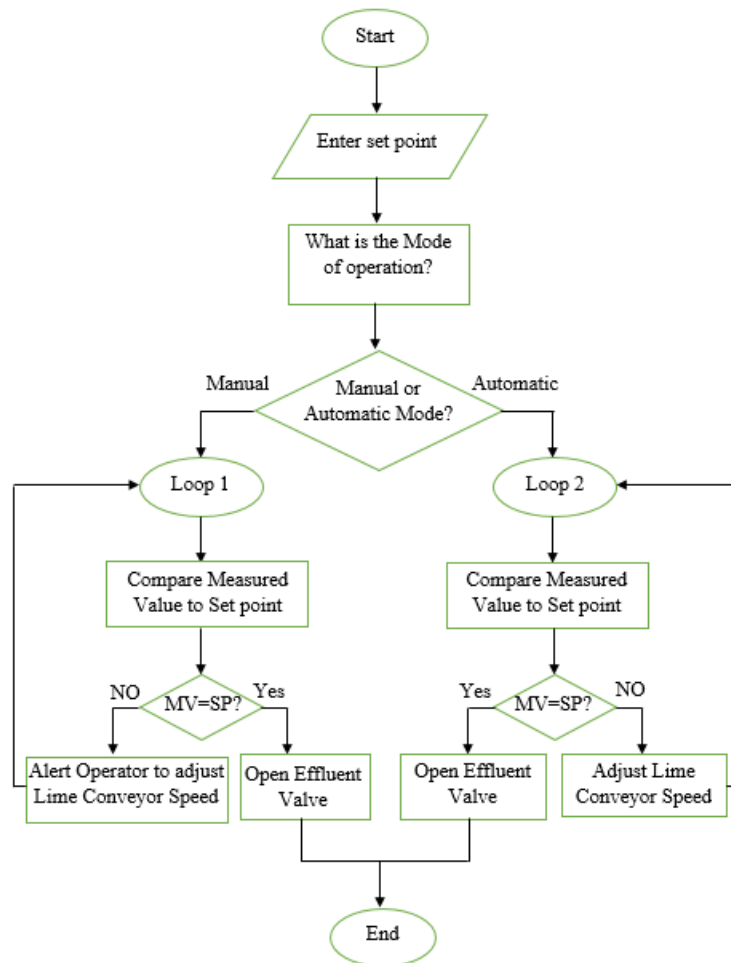


Figure 3. Logic flowchart of CoagiT

The designing phase in the development of CoagiT covered two main areas. They are:

- 1) Design of flowchart; and
- 2) Development of graphical user interface (GUI) of CoagiT.

3.2.1 Logic flowchart design

To determine graphically the logical steps involved in the execution of CoagiT, a standard flowchart was designed using standard logic flowchart symbols as shown in Figure 3.

3.2.2 Development of Graphical User Interface (GUI) of CoagiT

The GUI of CoagiT consist mainly of a user control section and a simulation section. The user control section was developed using Visual Basic controls such as; buttons, textboxes and radio buttons. The simulation section was also developed by using Visual Basic controls such as progress bars and track bars. Other Visual Basic controls such as labels, group boxes and the picture box found on the GUI were added to give information about the system to users.

3.3 Coding of CoagiT

After designing CoagiT's GUI and logic flowchart of the system, codes were written with Visual Basic (Visual Studio 2012) to bring the programme to operation. Declaration statements, conditional statements (such as if-then statements) and mathematical functions are some elements that constituted the codes. In effect, about four hundred (400) lines of programming codes were used in building CoagiT.

3.4 Debugging and Testing of CoagiT

Debugging of CoagiT was carried out to detect and correct errors in logic and syntax that were associated with running the programme. CoagiT was also tested using both alpha and beta testing mechanisms. The alpha testing was carried out by going through all the code lines to ensure that the correct syntax of Visual Basic was used. This was carried out during the coding section. Beta testing was also carried out to ensure that the programme responds and operates effectively as planned. CoagiT was also run on computers with different operating systems to test how it operates on these systems. Through the test, it was found out that, CoagiT operates best on Windows 7, 8 and 10 but does not run on Apple Macintosh operating systems and Android operating systems.

4 Results and Discussion

4.1 Operation of CoagiT

CoagiT measures the pH of the solution upon the addition of the coagulant. This measured pH is normally below the set point and as such the application triggers the addition of lime to the solution (by adjusting the speed of the lime conveyor motor) to bring the pH back to the set point. CoagiT has options to operate either in the manual mode (closed-loop, manual control) or in the automatic mode (closed-loop, automatic control). When operating in the manual mode (i.e. in the absence of a pH indicating controller), CoagiT has been designed to accept pH measurements from a transmitter and compare it with the set point. If there are any deviations, it triggers an alarm to alert plant operators of the possible deviation and as well suggest to plant operators the percentage by which the speed of the lime conveyor motor be adjusted to obtain the set point. Plant operators can adjust the speed of the lime conveyor motor from the application until the required coagulation pH is achieved.

In the automatic mode, CoagiT accept measurements from a transmitter, compares it with the set point and adjusts the speed of the lime conveyor motor automatically depending on the measured value using the pH indicating controller. This ensures that the optimum coagulation pH is achieved.

4.2 Graphical User Interface (GUI) of CoagiT

The Graphical User Interface (GUI) of CoagiT was designed in such a way, that it is simple and easy to

operate. It is made up of user controls and a simulation section (Figure 4). The simulation section consists of controls (such as the progress bar) to show the flow of raw water (influent) into the system and coagulated water out of the system. When CoagiT is running, the progress bar depicts the flow of water through the system with a green colour code. The simulation section also has radio buttons to allow/restrict the flow of water out of the system. User controls found on the GUI of CoagiT accept inputs or actions from users to function. Other controls such as labels and the picture box found on the GUI provides information about the system to users. Figure 4 below shows the Graphical User Interface (GUI) of CoagiT when the process has not started running.

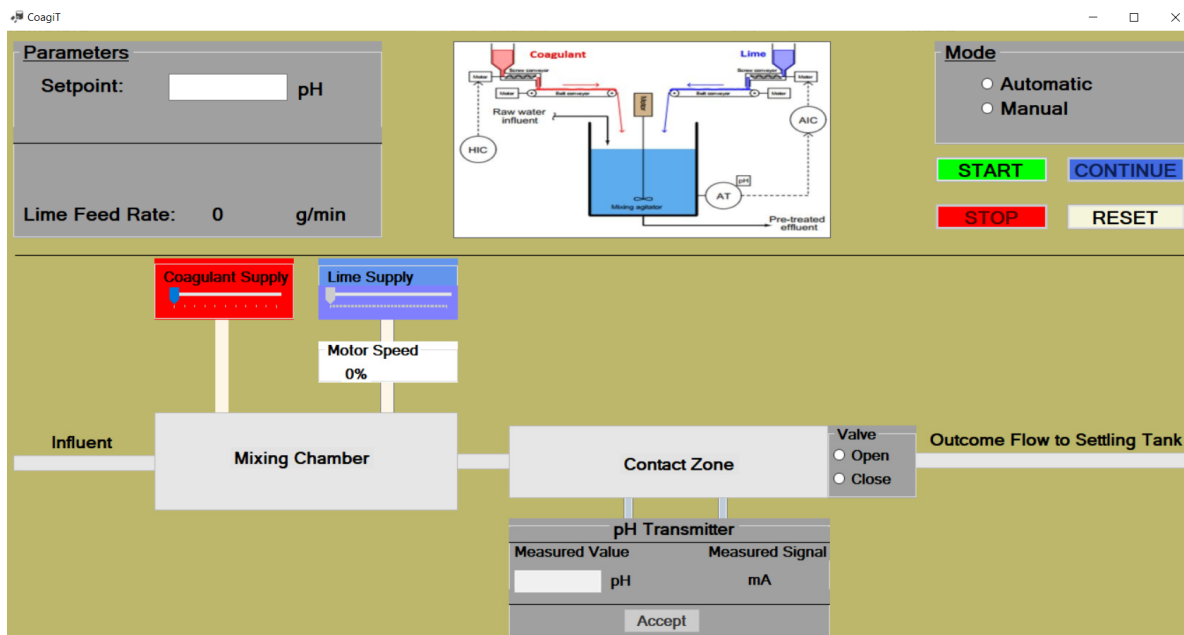


Figure 4. GUI of CoagiT after Loading

4.2.1 User controls

User controls found on the GUI of CoagiT include buttons, radio buttons, textboxes and a track bar. The buttons and their uses are explained in Tables 1 below.

4.3 Demonstration of CoagiT

During start up, raw water (influent) enters into the mixing chamber (this is seen on the GUI as described in section 4.2). Coagulant is added to the influent in this chamber. The addition of coagulant is confirmed by the change in value of the track bar at the coagulant supply and the change in colour of the discharge pipe carrying the coagulant to the mixing chamber on the GUI (the colour of the discharge pipe changes to red as shown in Figure 5). The solution (raw water and coagulant) then flows into the contact zone where there is a pH transmitter to measure and record the pH of the solution. Actions are taken depending on the mode of operation of the programme.

4.3.1 Automatic mode

In the automatic mode, when coagulant addition causes the measured pH value to fall below the set point, the software automatically adjusts the lime feed rate by adjusting the speed of the lime conveyor motor (i.e., the track bar on the lime supply automatically adjust to the desired lime supply rate percentage). This adjustment in lime supply would raise the measured pH value back to the set point thereby ensuring that the optimum coagulation pH necessary for effective coagulation is maintained. For example, assuming a set point of 6.5 pH is entered and the measured pH value after the addition of the coagulant is 1.5 (as illustrated in Figure 5), then an equivalent electrical signal of the measured value (in this case 7.69 mA) would be sent to the pH analytical controller. The pH analytical controller would

calculate the error/deviation and send a control signal to adjust the speed of the lime conveyor motor to 77% (as shown in Figure 6). This adjustment in motor speed would also change the lime feed rate to 669.90 g/min as shown in Figure 6. The large deviation of the measured value from the set point resulted in the application adjusting the speed of the lime conveyor motor to as much as 77% since more of the lime would be needed to bring the measured pH value back to the set point (as shown in Figure 6).

Table 1. Functions of user controls found on the GUI of CoagiT

User Control	Purpose
Radio Button	CoagiT uses radio buttons to select the mode of operation (automatic or manual) and to show the state of the outlet valve (i.e. open or close)
Textboxes	There are two textboxes on the GUI of CoagiT to accept set point and measured value inputs. In order to ensure efficient operation of the application, the textboxes are programmed to reject inputs other than numeric characters and also accept inputs that are only in the range of applicability.
Track Bar	The track bars found on the GUI are used to adjust the speeds of the conveyor motors carrying the lime and the coagulant.
Start Button	When clicked, the start button starts the flow of the influent through the mixing chamber to the contact zone in the simulation section.
Accept Button	Upon clicking, this button accepts the measured value input from the pH sensor and converts it to the required signal that will be transmitted to the pH indicating controller.
Continue Button	This button gives command depending on the mode of operation of CoagiT. In the automatic mode, the continue button upon clicking adjusts the speed of the lime conveyor motor and as well resume the flow of water in the simulation section. In the manual mode, the continue button upon clicking gives the percentage speed by which the lime conveyor motor need to be adjusted.
Apply Button	This button pops up when the continue button is clicked in the manual mode. When clicked, the apply button applies the adjusted speed of the lime conveyor motor and resumes the flow of water in the simulation section.
Stop Button	When clicked, this button stops the flow of water in the simulation section of the GUI of CoagiT.
Reset Button	When clicked, the reset button resets all inputs to default. It also clears the water in the simulation section.

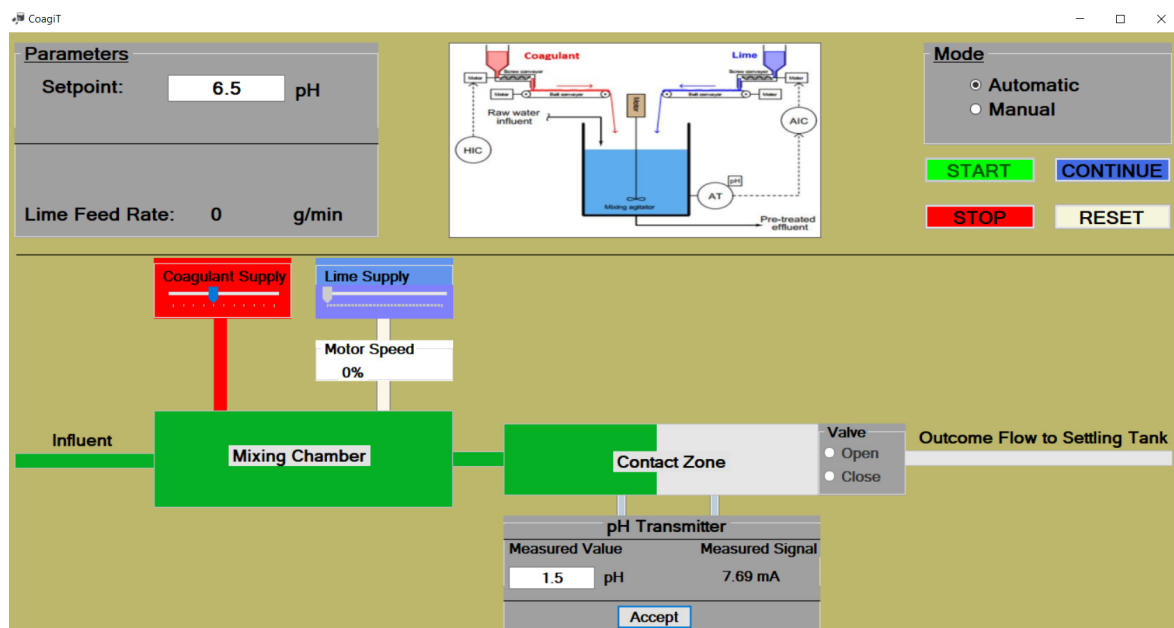


Figure 5. GUI when measured value is 1.5 pH (automatic mode)

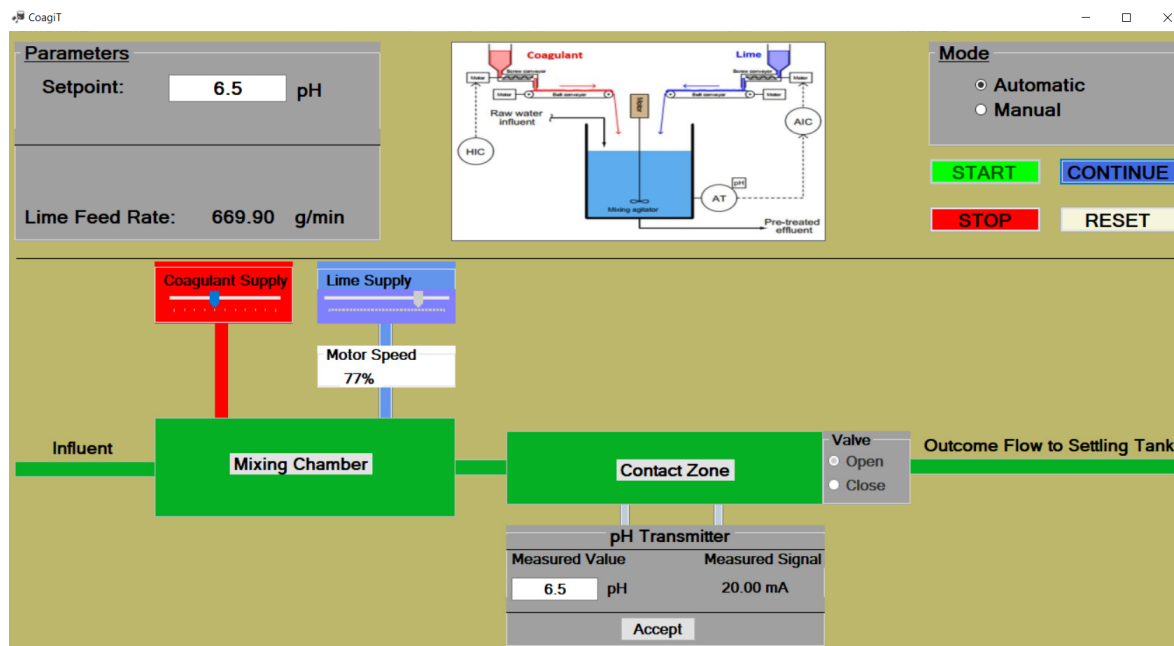


Figure 6. GUI after the lime conveyor motor speed has been adjusted to 77% (Automatic Mode)

In cases where there is a small deviation of the measured value from the set point, then the speed of the lime conveyor motor would be adjusted in the same magnitude as the deviation. Example, when a set point of 6.5 pH is entered and the measured pH value recorded after coagulant addition is 6.2 (as shown in Table 2), an equivalent electrical signal of 19.26 mA would be sent to the pH analytical controller. The pH analytical controller would calculate the error/deviation and send a control signal to adjust the speed of the lime conveyor motor and lime feed rate to 5% and 43.50 g/min respectively (as shown in Table 2). These adjustments in motor speed and lime feed rate would bring the measured pH value back to the set point. When the measured pH value is equal to the set point (pH = 6.5), the application would automatically open the outlet valve to allow the coagulated water flow to other process unit (such as the settling tank).

Table 2. Application results of CoagiT operating within a set point pH of 6.5

Measured Value (pH)	Measured Signal (mA)	Lime Conveyor Motor Speed (%)	Lime Feed Rate (g/min)	Measured Value (pH) after Lime Addition
1.5	7.69	77	669.90	6.5
2.5	10.15	62	539.40	6.5
4.5	15.08	31	269.70	6.5
5.5	17.54	15	130.50	6.5
6.2	19.26	5	43.50	6.5
6.5	20.00	0	0.00	6.5

4.3.2 Manual mode

When operating in the manual mode (i.e. in the absence of an analytical indicating controller), the application's main tasks are to:

- Alert plant operators of any possible deviation of the measured value from the set point by sounding an alarm and reading out a statement to the operators that, "coagulation pH is not achieved"; and
- Suggest to operator the percentage by which the speed of the lime conveyor motor should be adjusted to achieve the set point (i.e., the operator will manually move the track bar on the lime supply to the suggested percentage by the software).

When the pH transmitter (after the addition of the coagulant) records a pH value other than the set

point, a window form will appear on the GUI of the application with a message instructing operators to manually adjust the speed of the lime conveyor motor to a value depending on the magnitude of the error. For example, when a set point of 6.5 pH is entered and the pH transmitter (after coagulant addition) records a pH value of 2.0 with a signal of 8.92 mA, the programme would calculate the error and through the pop-up window displayed (serving as indicating controller), it will instruct operators to manually adjust the speed of the lime conveyor motor to 69% (as shown in Figure 7). After adjusting the lime conveyor motor to 69%, the user then clicks on apply for the process to proceed. As can be seen in Figure 8, the set point (pH =6.5, 20 mA) is attained when the speed of the lime conveyor motor was adjusted to 69%.

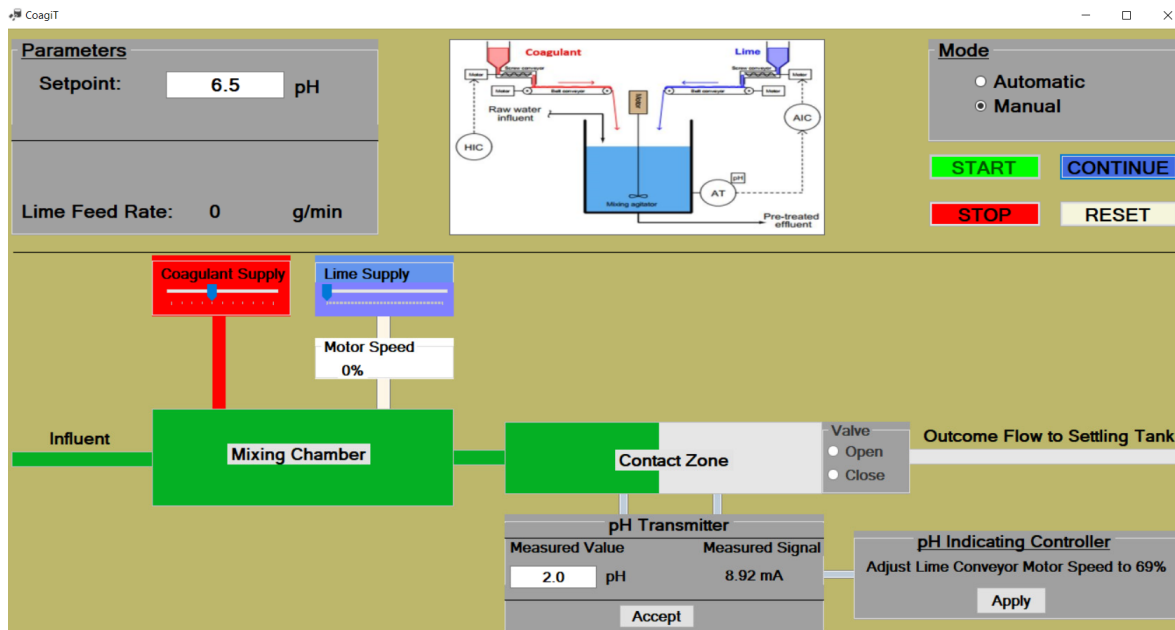


Figure 7. GUI when measured value is 2.0 pH (manual mode)

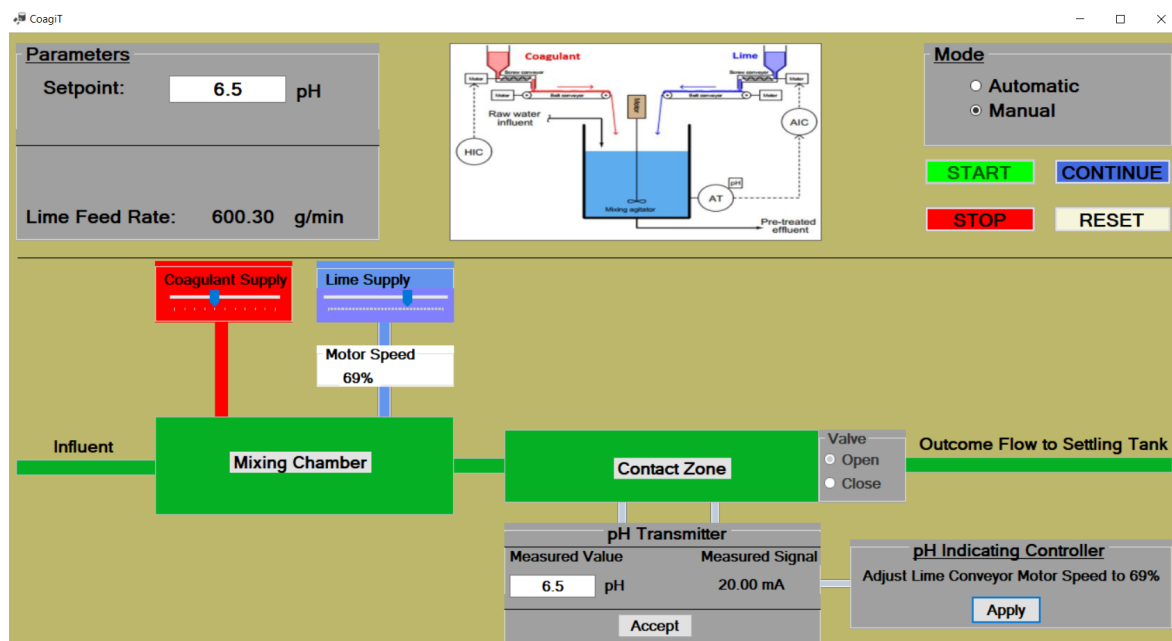


Figure 8. GUI after the lime conveyor motor speed has been manually adjusted to 69%

4.4 Limitations of CoagiT

VB has only discrete track bars and as a result of this the motor speed only shows integers by rounding up decimals. Also, VB lacks controls that represent the movement of conveyor belts and water tanks. As a result, simulating the PFD in Figure 1 was quite difficult. The application works within the following range of parameters: set-point of (6.5 - 8.5) pH; and measured value of (0 - Set point) pH.

5 Conclusions

A theoretical coagulation pH control simulation application called CoagiT has been successfully developed using process control principles and Visual Basic Programming Language. The main purpose of the application was to ensure effective simulation of coagulation in water treatment by maintaining the desired coagulation pH. The application is capable of operating in closed-loop, automatic control and closed-loop, manual control modes. It measures, alerts and predicts the dosing rates of lime required to maintain the desired coagulation pH using feedback control mechanisms. It is recommended that, the output of CoagiT should be controlled by standard algorithms in Process Control such as the Proportional-Integral-Derivative (PID) algorithm in controller and smart sensors to manage and eradicate errors effectively.

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References

1. Linder, K. and Zachman, B. (2009) "Getting Optimized: Optimize Coagulation and Flocculation", American Water Works Association, Vol. 35, No. 4, pp. 8-9.
2. Bello, O., Hamam, Y., and Djouani, K. (2016), "A comparative study of prediction models for Coagulation process in drinking Water Treatment Plants", Int. Journal of Applied Sciences and Engineering Research, Vol. 5, No. 6, pp. 1-9, ISSN 2277-9442.
3. Cox, C., Fletcher, I. and Adgar, A. (2001), "ANN-based sensing and control in the water industry: A decade of innovation", In Proceedings of the IEEE International Symposium on Intelligent Control, Mexico City, Mexico.
4. Koohestanian, A., Hosseini, M. and Abbasian, Z. (2008), "The separation method for removing of colloidal particles from raw water", American-Eurasian Journal of Agricultural and Environmental Science, Vol. 4, No. 2, pp. 266-273.
5. Anon. (2018), "Conventional Treatment", <https://iaspub.epa.gov>. Accessed: February 4, 2018.
6. Gebbie, P. (2006), "An operator's guide to water treatment coagulants", In 31st Annual QLD Water Industry Workshop—Operations Skills, University Central Queensland – Rockhampton, pp. 14-20.
7. Minkah, P.E., Fosu, S., Ndur, S.A., Asante, E.O., 2018. Computer simulation and modelling of chlorine monitoring and regulation system in water and wastewater treatment, 3 (1), pp. 69-78.
8. Ashery, A.F., Radwan, K. and Rashed, M.I.G. (2011), "The effect of pH control on turbidity and NOM removal in conventional water treatment", In Proceedings of the Fifteen International Water Technology Conference, Alexandria, Egypt, pp. 28-30.
9. Bourke, N., Carty, G., O'Leary, G., Crowe, M., Page, D. (2002), "Water Treatment Manuals-Coagulation, Flocculation & Clarification", Published by the Environmental Protection Agency, Ireland, pp. 14-19, ISBN: 1-84095-090-0.
10. BaiChuan, C., BaoYu, G., ChunHua, X., Ying, F., Xin, L. (2009), "Effects of pH on coagulation behaviour and floc properties of Yellow River water treatment using ferric based coagulants", Chinese Science Bulletin, Vol. 55, No. 14, pp. 1382-1387.
11. Hu, C., Liu, H., Qu, J., Wang, D. and Ru, J. (2006), "Coagulation behavior of aluminum salts in eutrophic water: significance of Al13 species and pH control", Environmental science & technology, pp. 325-331.
12. Kuphaldt, T.R. (2008), "Lessons in Industrial Instrumentation" Creative Commons Attribution/PA Control. Com, pp.491-2512.